

April 11, 2016

Remainder Theorem?

If $\frac{p(x)}{x-c}$, then $p(c) =$ a remainder

Factor Theorem

If $p(c) = 0$ Remainder!
then $x-c$ is a factor of $p(x)$

Apr 11-10:58 AM

Rational Zeros

$\frac{p}{q} = \frac{\text{factors of the constant term}}{\text{factors of the leading coefficient term}}$

$2x^3 - 4x^2 + 10$
 $p = 10$ & $q = 2$
 $10 = \pm 1, \pm 2, \pm 5, \pm 10$
 $2 = \pm 1, \pm 2$

$\frac{p}{q} = \pm \frac{1}{1}, \pm \frac{2}{1}, \pm \frac{5}{1}, \pm \frac{10}{1}, \pm \frac{1}{2}, \pm \frac{2}{2}, \pm \frac{5}{2}, \pm \frac{10}{2}$

$\frac{p}{q} = \pm 1, \pm 2, \pm 5, \pm 10, \pm \frac{1}{2}, \pm \frac{5}{2}$

Apr 11-11:09 AM

1 $\begin{array}{r} 2 \quad -4 \quad 0 \quad 10 \\ \underline{2 \quad -2 \quad -2} \\ 2 \quad -2 \quad -2 \quad -8 \end{array}$ $\begin{array}{r} 2 \quad -4 \quad 0 \quad 10 \\ \underline{10 \quad 30} \\ 2 \quad 6 \quad 30 \end{array}$

2 $\begin{array}{r} 2 \quad -4 \quad 0 \quad 10 \\ \underline{4 \quad 0} \\ 2 \quad 0 \quad 0 \quad 10 \end{array}$ $\begin{array}{r} 2 \quad -4 \quad 0 \quad 10 \\ \underline{1 \quad -2 \quad -3} \\ 2 \quad -3 \quad -3 \end{array}$

-10 $\begin{array}{r} 2 \quad -4 \quad 0 \quad 10 \\ \underline{-20 \quad 240} \\ 2 \quad -24 \quad 240 \end{array}$ $\begin{array}{r} 2 \quad -4 \quad 0 \quad 10 \\ \underline{-1 \quad -2 \quad -3} \\ 2 \quad -5 \quad -3 \end{array}$

$-\frac{1}{2} \cdot \frac{10}{2} = \frac{-5}{1}$

RM $\begin{array}{r} 2 \quad -4 \quad 0 \quad 10 \\ \underline{10 \quad 15 \quad 25} \\ 2 \quad 6 \quad 15 \end{array}$ $\begin{array}{r} 2 \quad -4 \quad 0 \quad 10 \\ \underline{5 \quad 15} \\ 2 \quad -9 \quad 15 \end{array}$

RM $\cdot \frac{15}{1} = \frac{25}{2}$ $-\frac{5}{2} \cdot \frac{45}{2} = -\frac{225}{4}$

Apr 11-11:17 AM

$p(x) = x^3 - 3x + 2 \rightarrow 1 \ 0 \ -3 \ 2$

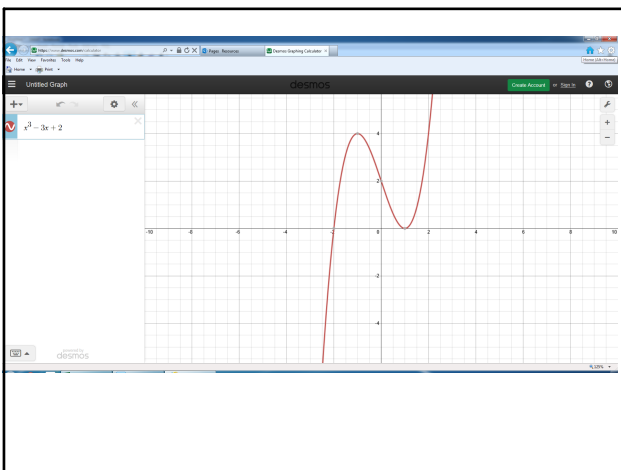
$p = 2 = \pm 1, \pm 2$
 $q = 1 = \pm 1$
 $\frac{p}{q} = \pm 1, \pm 2$

$p(1) = 0$ & $p(-2) = 0$
 $c = 1$ $c = -2$

$(x-1)(x^2+x-2)$
 factorable?
 $(x+2)(x-1)$
 $x^2 - x + 2x - 2$
 $x^2 + x - 2$

$f(x) = (x-1)(x+2)(x-1)$
 $x = 1, x = 2$

Apr 11-11:27 AM



Apr 11-11:52 AM